

Signal Analysis – Homework 02 (Signals)

1) – Determine E_∞ and P_∞ for:

a) $x(t) = \cos(t)$;

b) $x[n] = \cos(\pi n/4)$;

c) $x_1(t)$; given below in exercise 5;

d) $x_2(t)$; given below in exercise 7.

2) – a) – Show that $T_0 = (2\pi/a)$ is a **period** of $x_1(t)$ given below:

$$x_1(t) = b \cos(at + c)$$

b) – Show that $T_0 = (\pi/a)$ é um **period** de $x_2(t)$ given below:

$$x_2(t) = b |\cos(at)|$$

c) – Show that

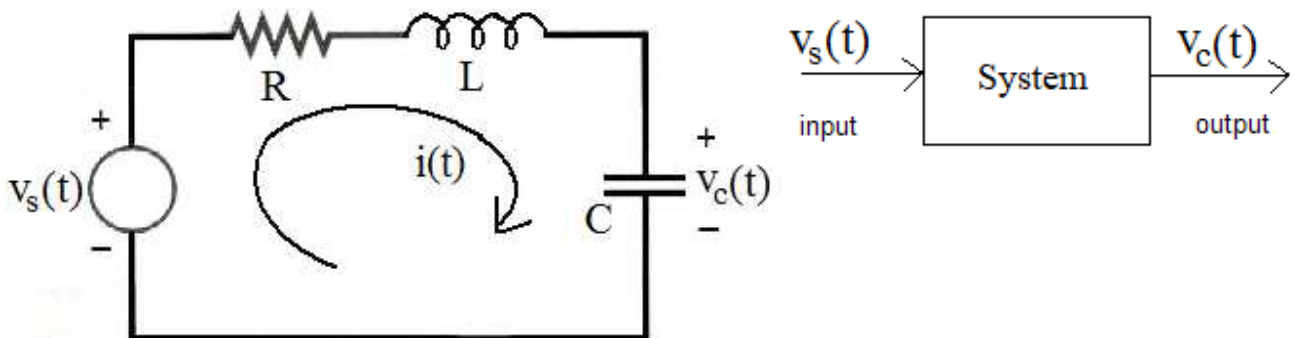
$$x(t) = e^{j3t} + e^{j6t}$$

$$= 2 e^{j4,5t} \cos(1,5t),$$

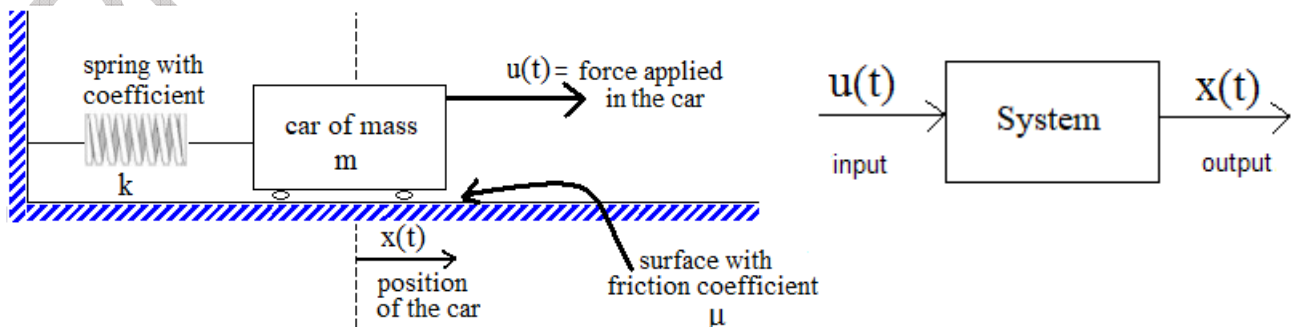
and therefore:

$$|x(t)| = 2 |\cos(1,5t)|.$$

3) – Find the **ODE (ordinary differential equation)** that describe the *electric SYSTEM* of the RLC circuit below where the input is $v_s(t)$ (source voltage) and the output is $v_c(t)$ (voltage in the capacitor).



4) – Find the **ODE (ordinary differential equation)** that describe the *mechanic SYSTEM* of the car-mass-spring given below where the input is $u(t)$ (force applied in the car) and the output is $x(t)$ (position of the car).



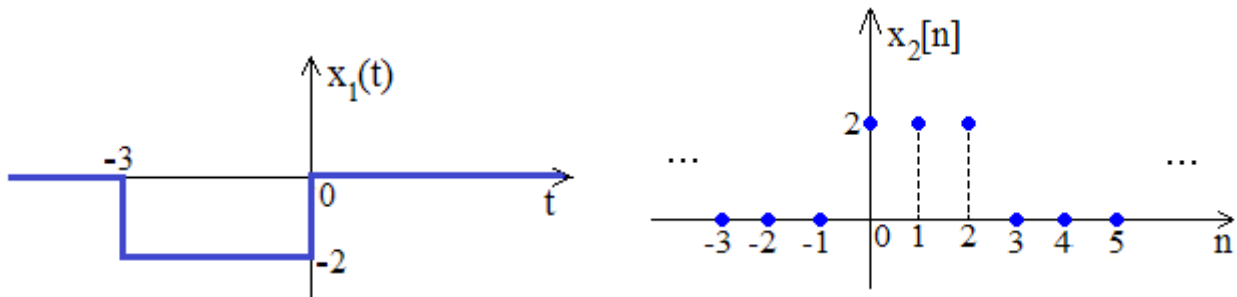
Signal Analysis – Homework 02
(Signals)

5) – Decompose the **continuous signal** $x_1(t)$ given below by the sum of 2 **signals**, one being **even** [$x_{1ev}(t)$] and the other one being **odd** [$x_{1od}(t)$].

6) – For $x_1(t)$ given below, make a sketch of $x_1\left(\frac{t}{2} - 2\right)$.

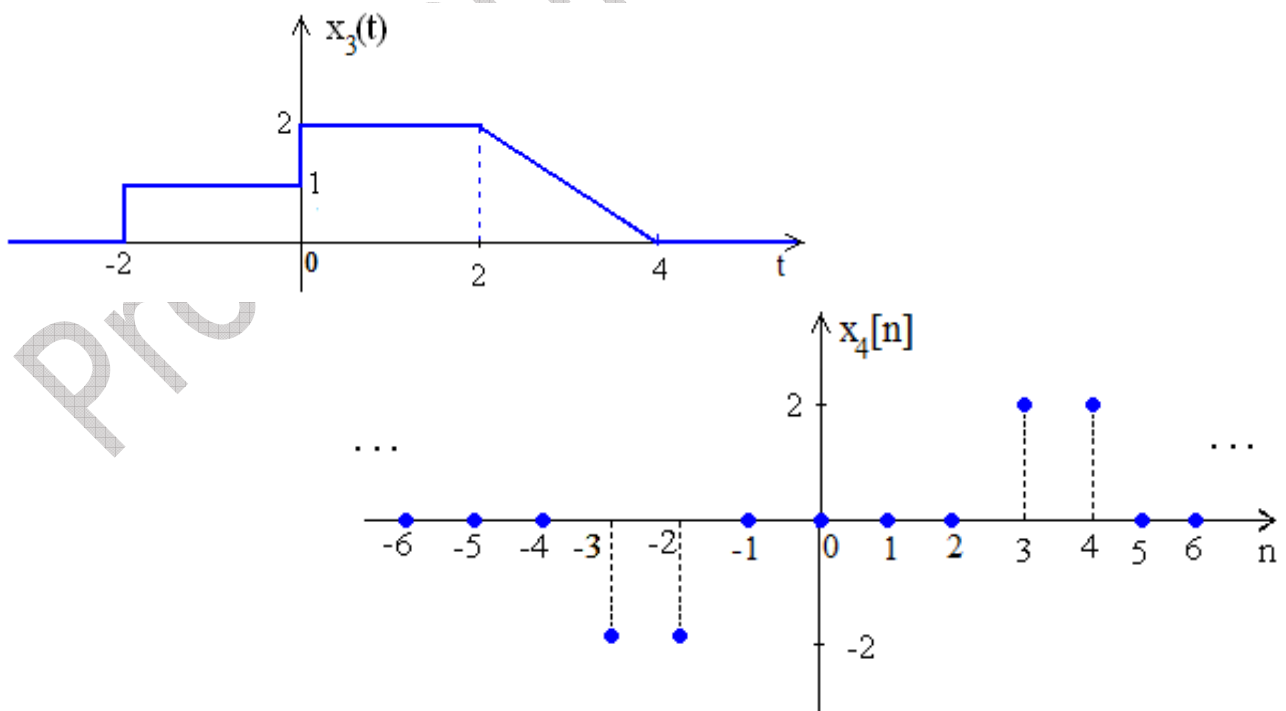
7) – Decompose the **discrete signal** $x_2[n]$ given below by the sum of 2 **signals**, one being **even** ($x_{2ev}[n]$) and the other one being **odd** ($x_{2od}[n]$).

8) – For $x_2[n]$ given below, make a sketch of $x_2\left(\frac{n}{3} + 1\right)$.



9) – Decompose the **continuous signal** $x_3(t)$ given below by the sum of 2 **signals**, one being **even** [$x_{3ev}(t)$] and the other one being **odd** [$x_{3od}(t)$].

10) – Decompose the **discrete signal** $x_4[n]$ given below by the sum of 2 **signals**, one being **even** ($x_{4ev}[n]$) and the other one being **odd** ($x_{4od}[n]$).



Signal Analysis – Homework 02
(Signals)

- 11) – For $x_3(t)$ given above, make a sketch of $x_3(2t+3)$.
- 12) – For $x_4[n]$ given above, make a sketch of $x_4\left[\frac{(t-2)}{2}\right]$.
- 13) – Show that the **signal** $x(t)$ described in the form of a linear combination of a **sine** and a **co-sine** with the same frequency $\omega_0 t$ and without phase displacement, can be written as a **sine** with the same frequency $\omega_0 t$ and phase displacement ϕ ; and vice-versa. That is:

$$\begin{aligned} x(t) &= \alpha \cdot \sin(\omega_0 t) + \beta \cdot \cos(\omega_0 t) \\ &= A \cdot \sin(\omega_0 t + \phi) \end{aligned}$$

where:

$$\begin{aligned} \alpha &= A \cdot \cos \phi & \text{and} & & \beta &= A \cdot \sin \phi \\ A &= \sqrt{\alpha^2 + \beta^2} & \text{and} & & \phi &= \arctg(\beta/\alpha) \end{aligned}$$

- 14) – For each one of the items below, find the values of a , b , c and θ que satisfy the equality presented.

a) – $x(t) = 3 \cos(at) + b \sin(2t) = 5 \cos(at + 36.86^\circ) = c \sin(at + \theta)$

b) – $x(t) = a \cos(bt + 36.86^\circ) = a \sin(2t + \theta) = 8 \sin(bt) + c \cos(bt)$

- 15) – Find the values of ϕ , k and θ that satisfy the equation below.

$$3,48 \cdot \cos(\theta t) = 8 \cdot \sin(2,7t + \phi) + k \cdot \sin(\theta t)$$

- 16) – Find the values of α , λ (in radians) and γ (in degrees) that satisfy the equation below.

$$12,5 \cdot \sin\left(\frac{3\pi}{2}t + 2\gamma\right) = \frac{\alpha}{2} \cdot \cos(2\lambda t) + 3\alpha \cdot \sin(2\lambda t)$$

- 17) – Find the values of α , of θ_1 and of θ_2 that satisfy the equation below.

$$\alpha \cdot e^{(\theta_1 t)} \cdot \cos(\theta_2 t) = (e^{-2jt} + e^{jt})$$

Signal Analysis – Homework 02
(Signals)

18) – Calculate the values of the β , θ_1 and θ_2 that satisfy the equation below.

$$\beta \cdot (e^{2jt} - e^{-5jt}) = 3,5 \cdot e^{j\theta_1 t} \cdot \sin(\theta_2 t)$$

19) – Write the **discrete periodic signals** $x[n]$ given below in terms of the trigonometric functions sine and co-sine.

